A Collaborative Proposal to the NSF Experimental Expeditions Program



Computational Biology of Cancer

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Our Vision



To gain fundamental new insights into the emergent behaviors of complex biological and embedded systems through the use of revolutionary, highly scalable, and fully automated modeling and analysis techniques.

Primary Challenge: Scalability



Key Scalability Issues:

Spatial Distribution

Stochastic Behavior

Highly Nonlinear Behavior

Mixed (Hybrid) Continuous-Discrete Behavior

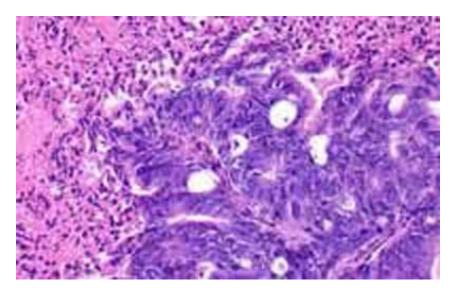
Vast Numbers of System State Variables & Components

Complex Biological & Embedded Systems can exhibit any combination of these features

Pancreatic Cancer



- 4th leading cause of cancer death in the US and Europe
- Five-year survival rate is only 4%
- Almost no progress in diagnosis and treatment in the past 40 years



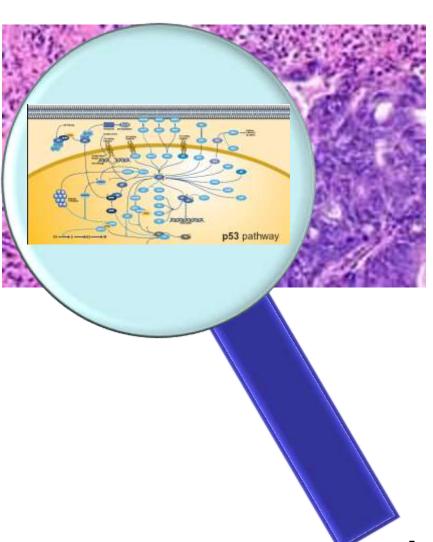
Healthy and diseased pancreas cells

New insights into the dynamics of these deadly diseases are urgently needed!

Why Pancreatic Cancer?



- No animal model, so computational models are needed
- Signaling models from cancer experts at TGEN (Translational Genomics)
- We will build new analysis and verification tools
- TGEN collaborators will use tools to better understand cancer dynamics



Model Checking



The Model Checking Problem:

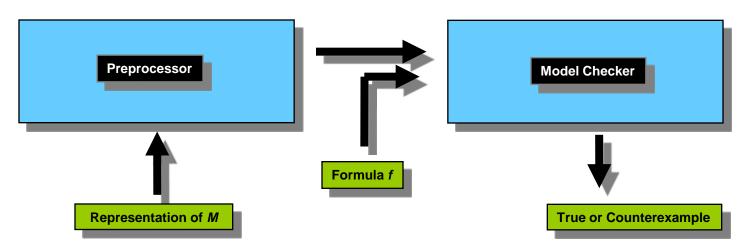
Let **M** be a **state-transition graph**

Let f be a formula of temporal logic

e.g., a U b means "a holds true Until b becomes true"



Does f hold along all paths that start at initial state of M?



Biological Models of Cancer



- Cancer as a disease of the genome...
- Cancer as a somatic evolutionary process...
- Cancer as a price of symbiosis (mitochondrial)...
- Cancer as a response to multi-cellularity...
- Cancer as a price of repair/regeneration (stem cells)...
- Cancer as a consequence of energy consumption (glucose metabolism)...
- Cancer as a response to external stress...
- Cancer as a response to the micro-environment (hyperand hypo-methylation)...

Relevant Biological Processes



- Proliferation:
 - Oncogenes and Tumor Suppressor Genes
- Differentiation:
 - Stem Cells...
- Signaling:
 - Kinases...
- Maintenance and Immortality:
 - Autophagy, Necrosis and Apoptosis

War on Cancer





"... as we know, there are known
 knowns; there are things we know we
 know.

"We also know there are **known** unknowns; that is to say we know there are some things we do not know.

"But there are also unknown unknowns

- the ones we don't know we don't know."
 - Ex-US Secretary of Defense, Mr. Donald Rumsfeld, Quoted completely out of context.

Known Known Biology



Theory: "World Where There Are Names for Everything."

"Addicted to Death"



- Cancer is a progressive switch from apoptotic (scheduled) to necrotic (unscheduled) tumor cell death.
- The immunobiology of many intracellular factors are involved:
 - the products of purine metabolism (<u>uric acid, ATP, and adenosine</u>);
 - the nuclear protein HMGB1; the S100 family members; the heat shock proteins;
- Cancer is the consequence of disordered tumor cell death rather than cell growth
 - Loss of homeostasis
 - A condition called "addicted to death."

Purine Metabolism



Purine Metabolism

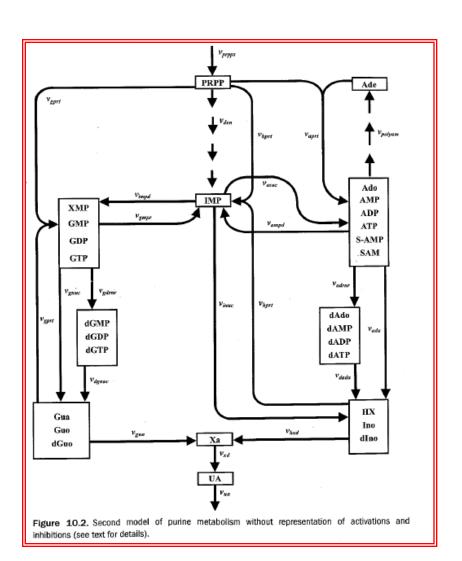
 Provides the organism with building blocks for the synthesis of DNA and RNA.

The entire pathway is almost closed but also quite complex. It contains

- several feedback loops,
- cross-activations and
- reversible reactions

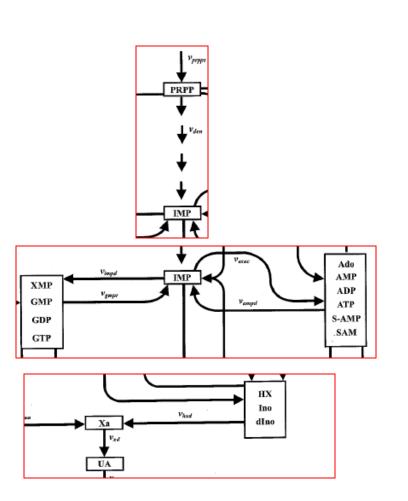
Simple Model





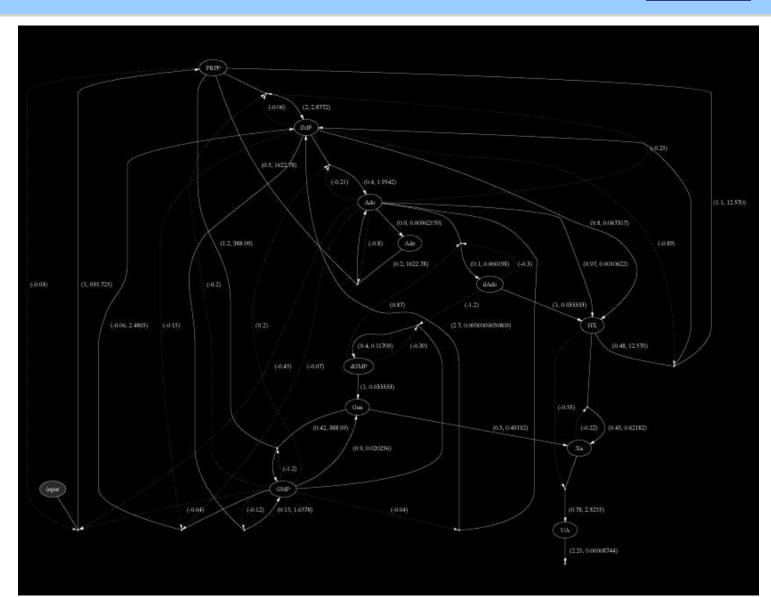
Biochemistry of Purine Metabolism





- The main metabolite in purine biosynthesis is 5-phosphoribosyl-a-1pyrophosphate (PRPP).
 - A linear cascade of reactions converts PRPP into inosine monophosphate (IMP).
 - IMP is transformed into AMP and GMP.
 - Guanosine, adenosine and their derivatives are recycled (unless used elsewhere) into hypoxanthine (HX) and xanthine (XA).
 - XA is finally oxidized into *uric acid* (*UA*).

urine Metabolism



Queries



Variation of the initial concentration of PRPP does not change the steady state.
 (PRPP = 10 * PRPP1) implies steady_state()

- Persistent increase in the initial concentration of PRPP does cause unwanted changes in the steady state values of some metabolites.
- If the increase in the level of PRPP is in the order of 70% then the system does reach a steady state, and we expect to see increases in the levels of IMP and of the hypoxanthine pool in a "comparable" order of magnitude.

Always (PRPP = 1.7*PRPP1) implies steady_state()





Queries



- Consider the following statement:
- Eventually (Always (PRPP = 1.7 * P

```
(Always (PRPP = 1.7 * PRPP1)
implies
steady_state()
and Eventually
Always(IMP < 2* IMP1))
and Eventually (Always
(hx_pool < 10*hx_pool1)))
```

- where IMP1 and hx_pool1 are the values observed in the unmodified trace.
- The model checker determines that the above statement is false...

- Counter-example: Model checker shows that the increase in IMP is about 6.5 fold while the hypoxanthine pool increase is about 60 fold.
- The model "over-predicts" the increases in products by amounts that are physiologically impossible...

 The model should therefore be amended



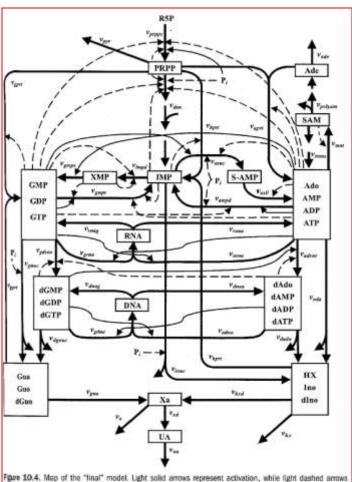
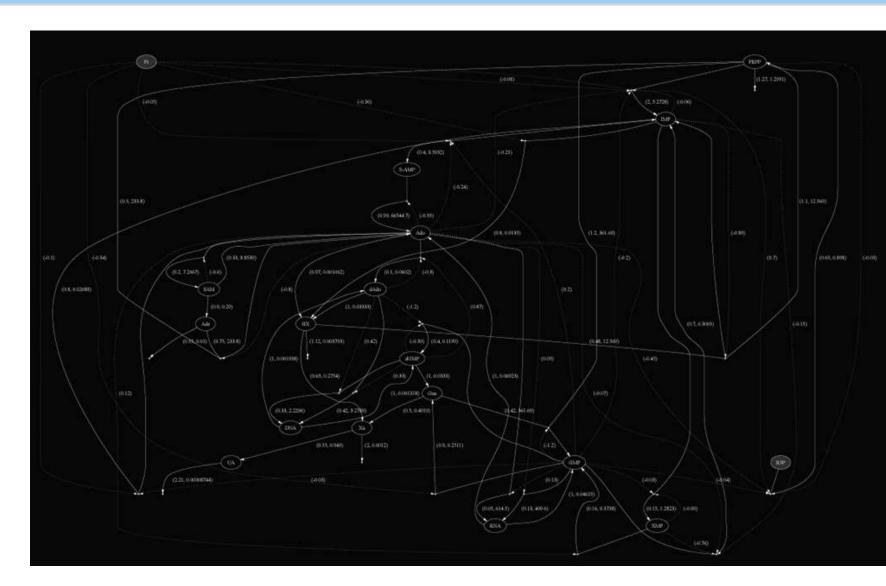


Figure 10.4. Map of the "final" model, Light solid arrows represent activation, while light dashed arrows represent inhibition. Curved heavy arrows entering or leaving the pathway indicate purine ring and ribose teleties that balance the stoichiometry of the system.

Purine Metabolism



XS-Systems:

(AAMC M. et al. 2001-2009)



Canonical Form:

$$\begin{cases} \dot{X}_{i} = \alpha_{i} \prod_{j=1}^{n+m} X_{j}^{g_{ij}} - \beta_{i} \prod_{j=1}^{n+m} X_{j}^{h_{ij}} & i = 1...n \\ C_{l}(X_{1}(t), ..., X_{n+m}(t)) = \sum_{j=1}^{n+m} (\gamma_{l} \prod_{j=1}^{n+m} X_{j}^{f_{lj}}) = 0 \end{cases}$$

Characteristics:

- Predefined Modular Structure
- Automated Translation from Graphical to Mathematical Model
- ♦ Scalability

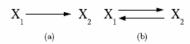


Figure 1: Representation of an unmodified and of a reversible reaction.

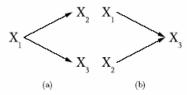


Figure 2: Representation of a divergence and of a convergence branch point (the two processes in each reaction are independent of each other).

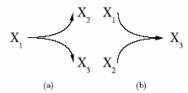


Figure 3: Representation of a single splitting reaction generating two products, X_2 and X_3 , in stoichiometric proportions and of a single synthetic reaction involving two source components, X_1 and X_2 always in stoichiometric proportions.

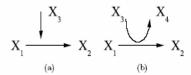
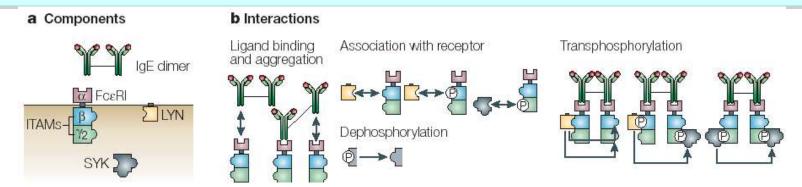


Figure 4: The conversion of X_1 into X_2 is modulated (stimulation or inhibition is represented by the sign of the arrow) by X_3 . The reaction between X_1 and X_2 requires coenzyme X_3 , which in the process is converted into X_4 .

Rule-based modeling protocol



1. Define components as *structured objects* and interactions as *rules*.



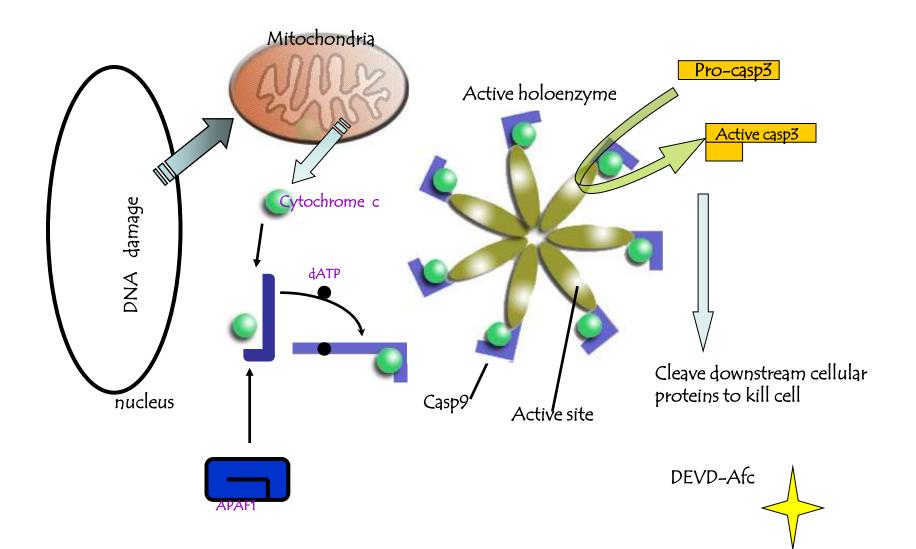
2. Determine concentrations and rate constants



3. Generate and simulate the model.

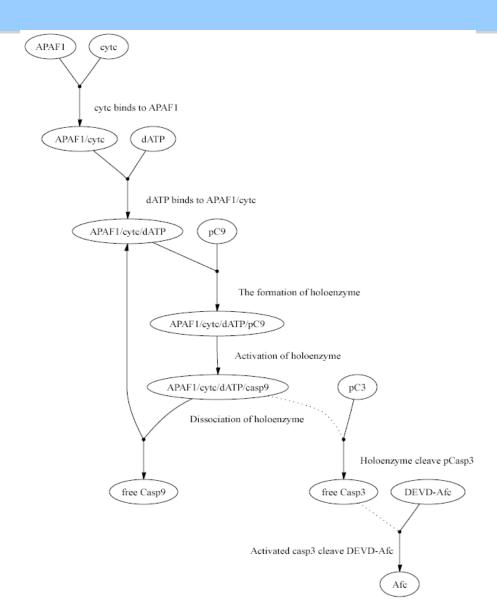
The activation of Casp9 needs APAF1 and cytochrome c





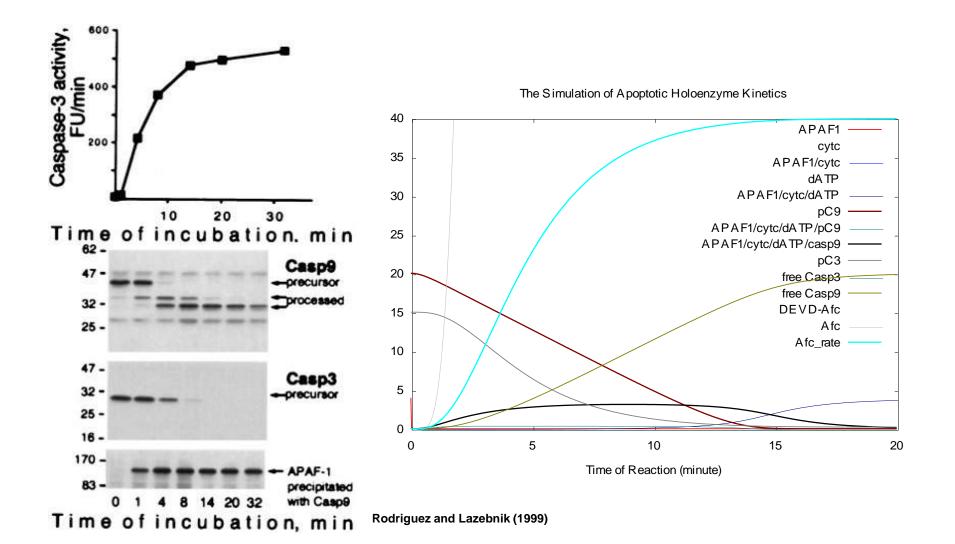
xS-System Model





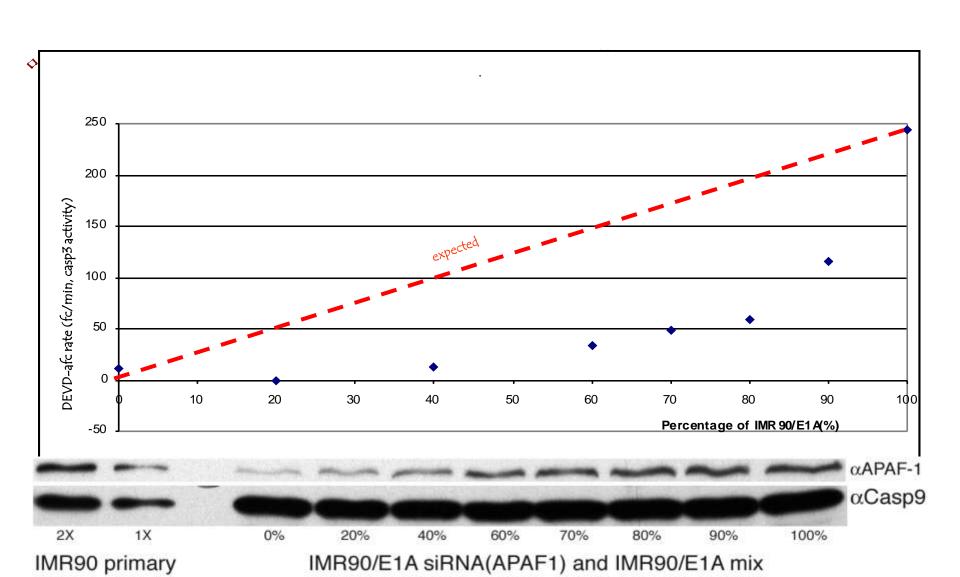
Simpathica recapitulate the holoenzyme formation process





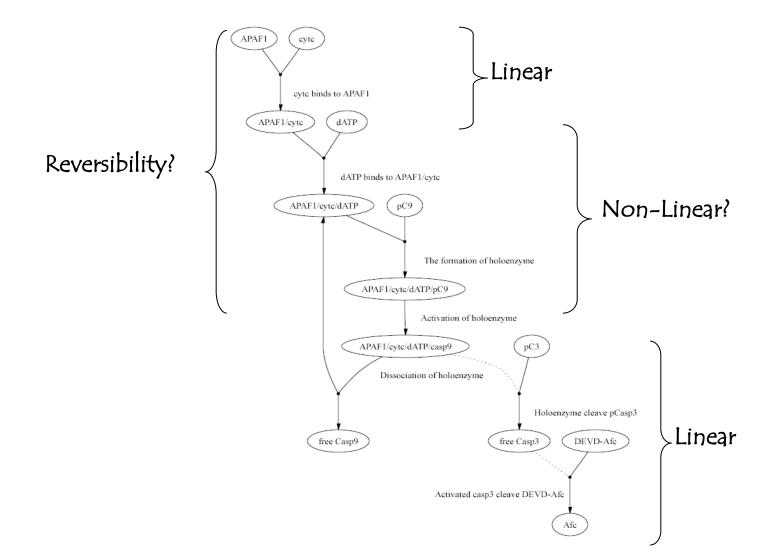
Decreasing [APAF-1] Kill Caspase Activity





Where to modify the model in Simpathica?

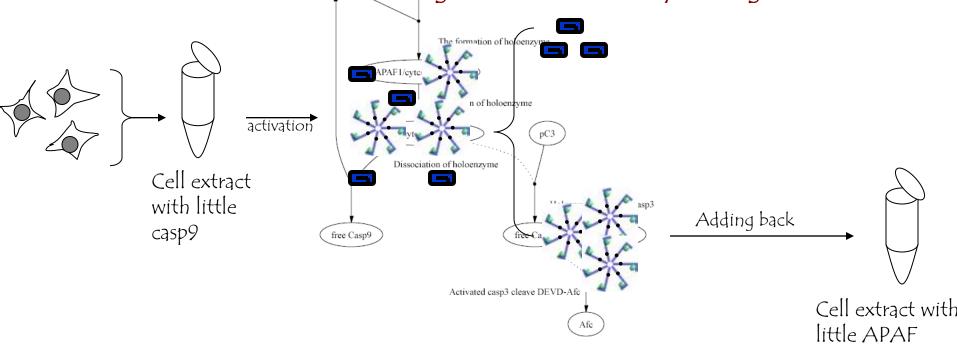








- ♦ Recombinant system:
 - cytochrome caspase-9, APAF1
- * Purification of endogenous APAF1/cytc oligomer



 $[APAF1/cytc/dATP] \rightarrow caspase3 activity$

Linear dependence?

XS-Systems:

(AAMC M. et al. 2001-2009)



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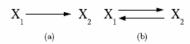


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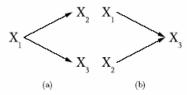


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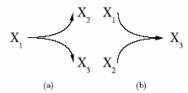


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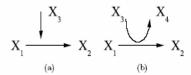


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Formal Definition of S-system

Definition 1 (S-system). An S-system is a quadruple S = (DV, IV, DE, C) where:

- $-DV = \{X_1, \ldots, X_n\}$ is a finite non empty set of dependent variables ranging over the domains D_1, \ldots, D_n , respectively;
- $-IV = \{X_{n+1}, \ldots, X_{n+m}\}$ is a finite set of independent variables ranging over the domains D_{n+1}, \ldots, D_{n+m} , respectively;
- DE is a set of differential equations, one for each dependent variable, of the form

$$\dot{X}_i = \alpha_i \prod_{j=1}^{n+m} X_j^{g_{ij}} - \beta_i \prod_{j=1}^{n+m} X_j^{h_{ij}}$$

with $\alpha_i, \beta_i \geq 0$ called rate constants;

- C is a set of algebraic constraints of the form

$$C_j(X_1,\ldots,X_{n+m}) = \sum (\gamma_j \prod_{k=1}^{n+m} X_k^{f_{j_k}}) = 0$$

with γ_i called rate constraints.

Verifying temporal properties of a reactive system



- Step 1. Formally encode the behavior of the system as a semi-algebraic hybrid automaton
- Step 2. Formally encode the properties of interest in TCTL
- Step 3. Automate the process of checking if the formal model of the system satisfies the formally encoded properties using quantifier elimination

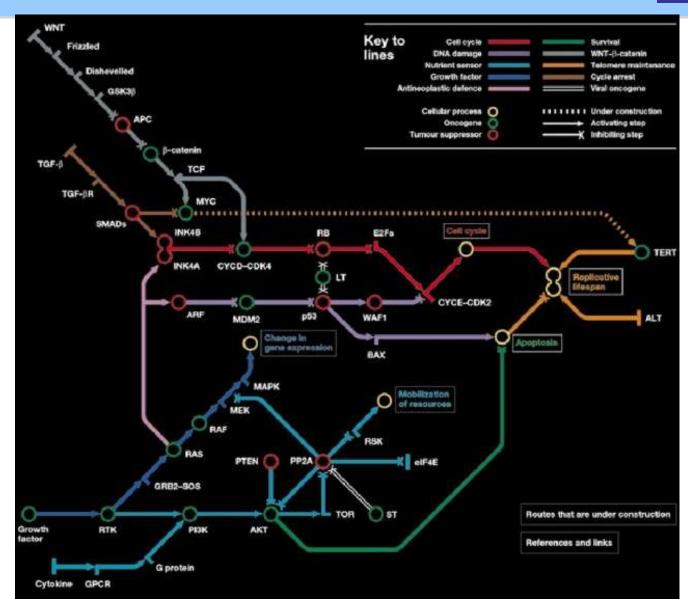
Solution



- Bounded Model Checking
- Constrained Systems
 - Linear Systems
 - O-minimal
 - SACoRe (Semi algebraic Constrained Reset)
 - IDA

Subway Map of Cancer





Is this View of Cancer Necessarily Accurate?





- "If I said yes, that would then suggest that that might be the only place where it might be done which would not be accurate, necessarily accurate.
- "It might also not be inaccurate, but I'm disinclined to mislead anyone."
 - Ex-US Secretary of Defense, Mr.
 Donald Rumsfeld, Once again quoted completely out of context.

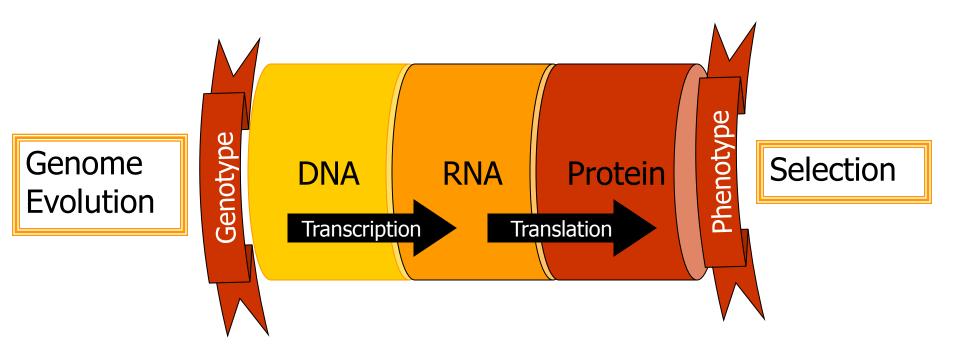
Known Unknown Biology



Reality: "World Where There Are No Names of Anything."

The New Synthesis





Cancer Initiation and Progression



Mutations, Translocations, Amplifications, Deletions

Epigenomics (Hyper & Hypo-Methylation)

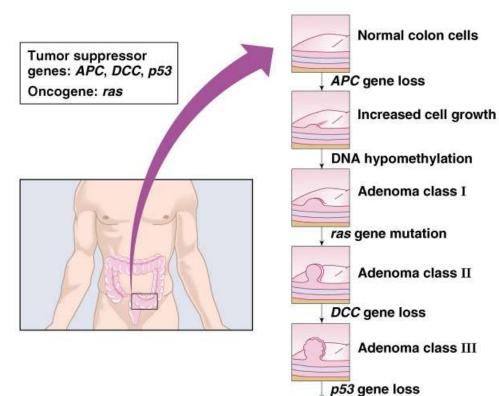
Alternate Splicing

Cancer Initiation and Progression

Proliferation, Motility, Immortality, Metastasis, Signaling, Microenvironment (autophagy)

Amplifications & Deletions





Carcinoma

Other gene losses

Metastasis

Mutation in a TSG

Epigenomics

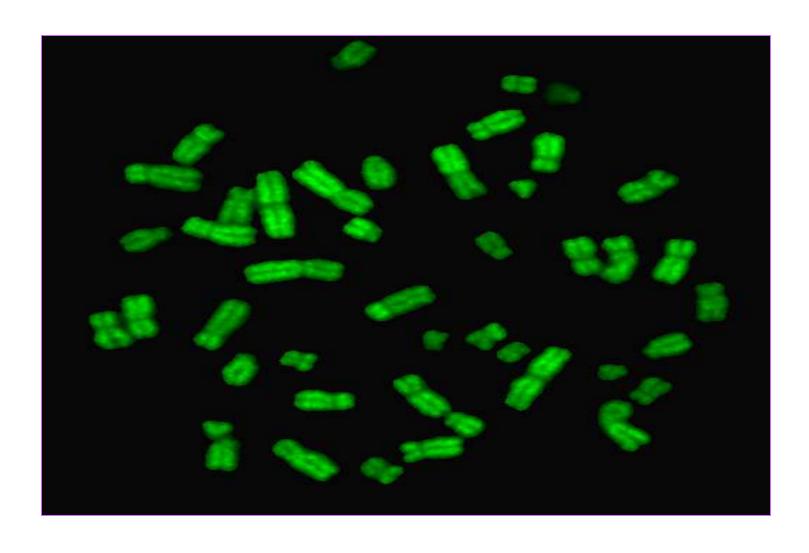
Conversion of a Proto-Oncogene

Deletion of a TSG

Deletion of a TSG

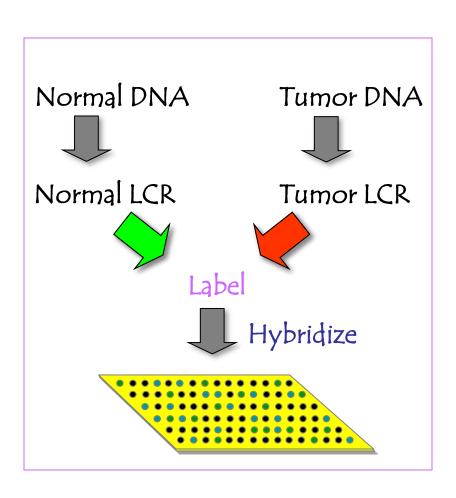
Karyotyping





Microarray Analysis of Cancer Genome

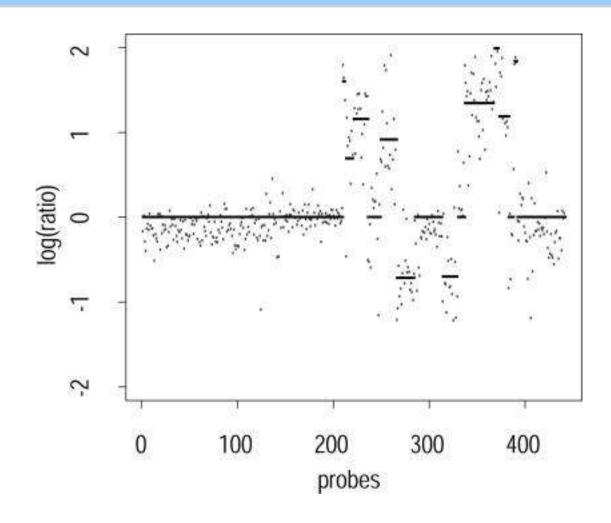




- Representations are reproducible samplings of DNA populations in which the resulting DNA has a reduced complexity.
 - Array probes derived from low complexity representations of the normal genome
 - We measure differences in gene copy number between normal and tumor samples ratiometrically

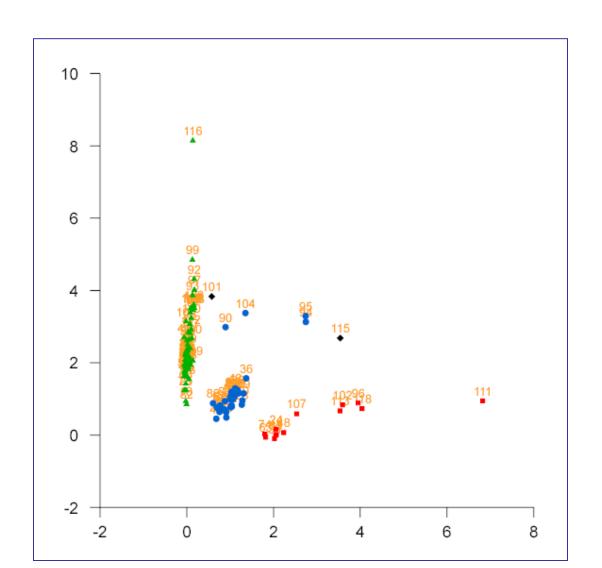
Daruwala et al. (PNAS, 2004)





Allelic Frequencies: Cancer & Normal (Anantharaman et al. unpublished)





Cell Stress: Glycosylation



- Some tumor-specific conditions (e.g., hypoxia, low pH and low level of glucose) commonly cause the glucoseregulated stress response of cancer cells.
- One can induce various stress responses in cancer cells artificially, and study them experimentally.
- For example, Tunicamycin induces (gylycosylation) stress:
 - It blocks the synthesis of all N-linked glycoproteins (N-glycans)
 - And causes cell cycle arrest in G1 phase.



Proprietary experimental results removed.

Concept (M. et al. 2006-2009)



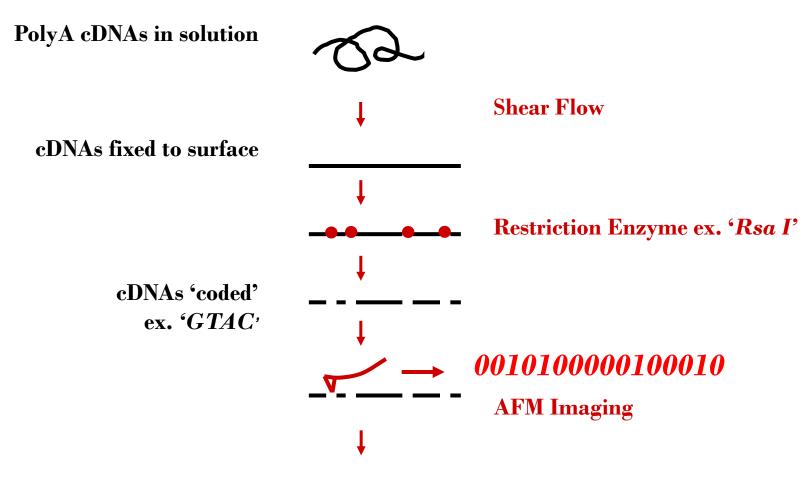
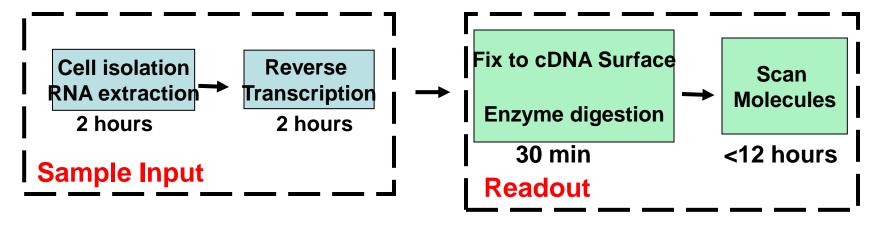


Image Processing, Pattern Matching

Single Molecule Restriction Map

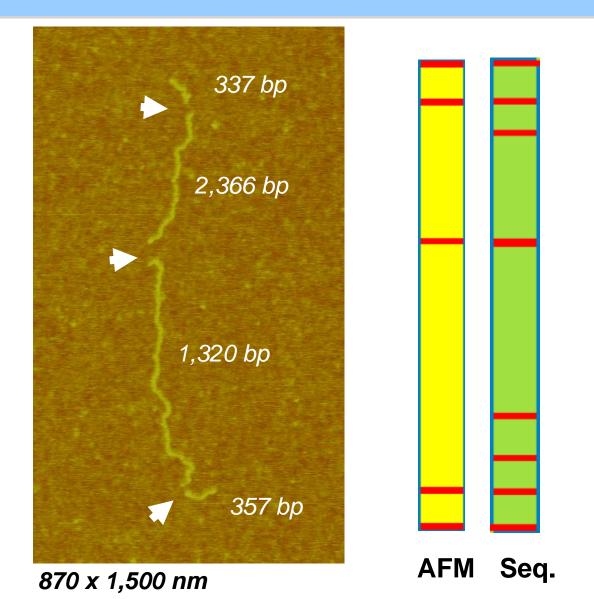




Microfluidic Device + Fast AFM

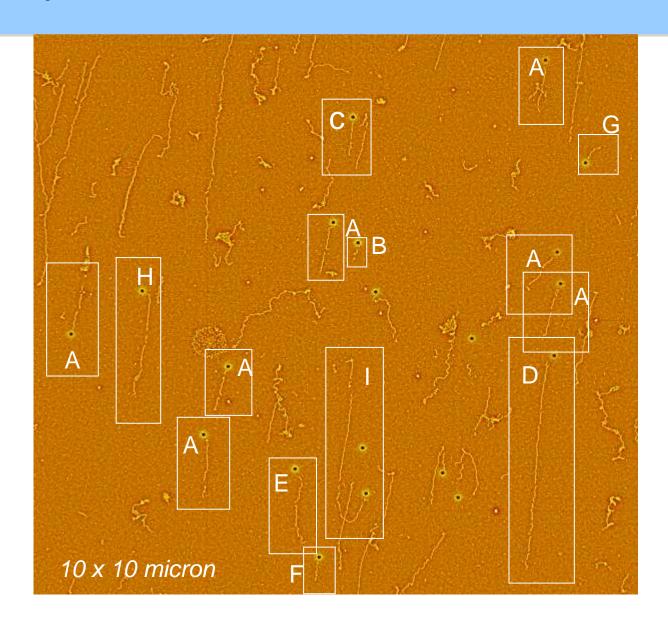
AFM vs Sequence





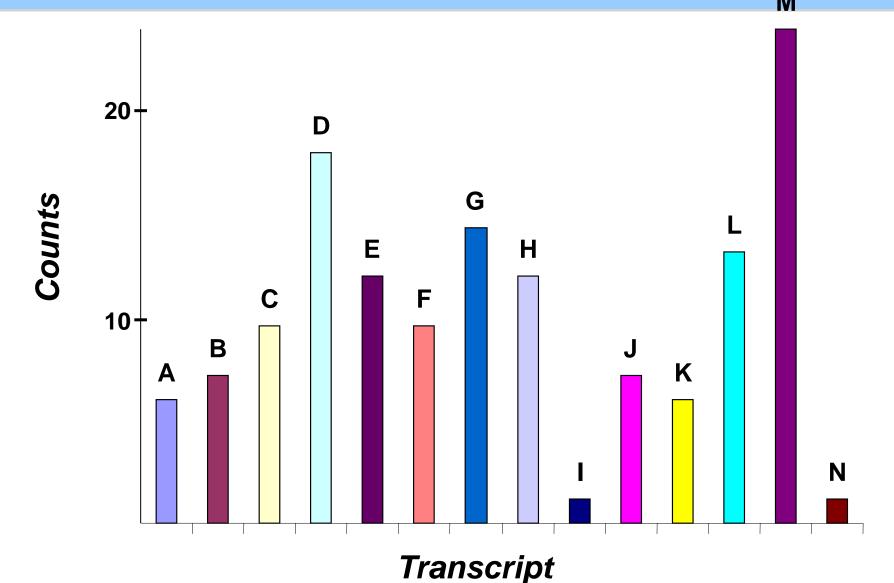
Identify and Count





Histogram of Transcript Abundance





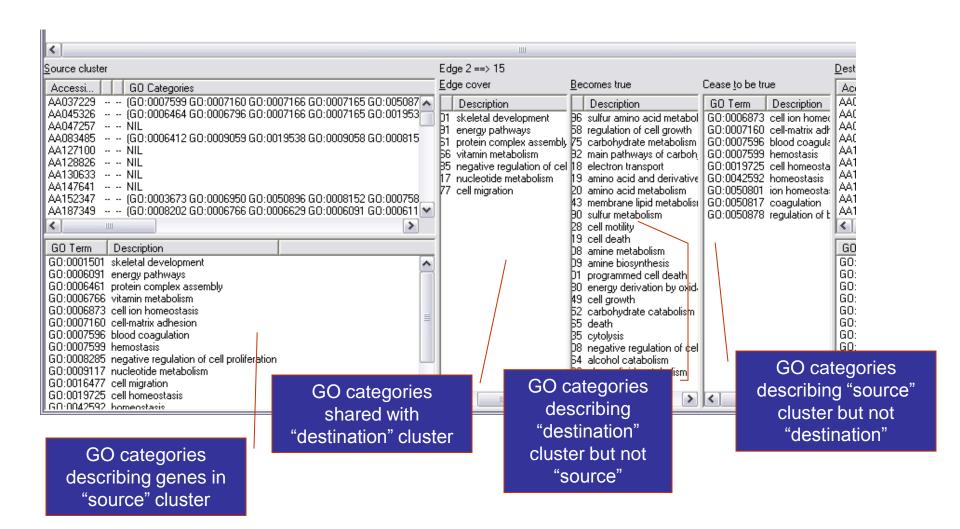
Models that are Concepty





- "I'm not into this detail stuff.
- "I'm more concepty."
 - Ex-US Secretary of Defense, Mr.
 Donald Rumsfeld, Once again quoted completely out of context.

GOALIE: GO Algorithmic Logic for Invariant Extraction

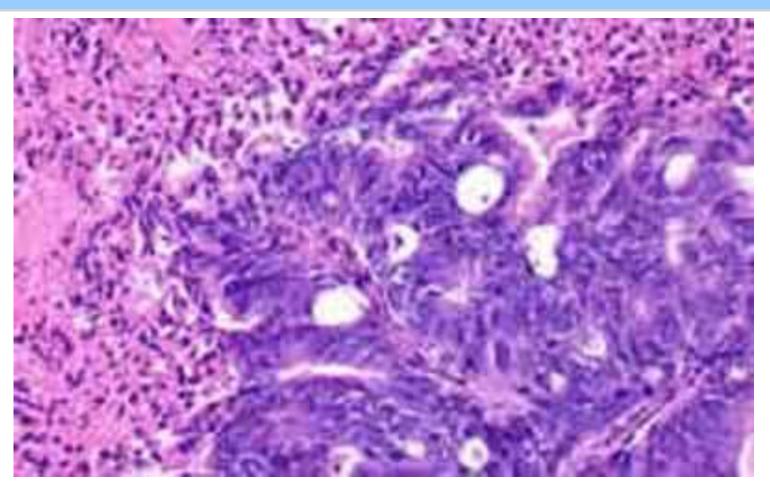


Unknown Unknown Biology



Pathologist's View





Healthy and diseased pancreas cells

A Challenge



- "At present, description of a recently diagnosed tumor in terms of its underlying genetic lesions remains a distant prospect. Nonetheless, we look ahead 10 or 20 years to the time when the diagnosis of all somatically acquired lesions present in a tumor cell genome will become a routine procedure."
 - Douglas Hanahan and Robert Weinberg
 - Cell, Vol. **100**, 57-70, 7 Jan 2000



Blast from the Past





- "I would not say that the future is necessarily less predictable than the past. I think the past was not predictable when it started."
 - Ex-US Secretary of Defense, Mr Donald Rumsfeld.

Foci



- Measurements
 - Single Cell Single Molecule Experiments
- Modeling & Model Checking
 - Phenomenological & Mechanistic Models
- Mining
 - Hypotheses
- Manipulation
 - Diagnostics and Therapeutics

Translational Systems Biology



- "A Sense of Life: Computational & Experimental Investigations with Models of Biochemical & Evolutionary Processes," (with R. Daruwala, Y. Zhou, N. Ugel, A. Policriti, M. Antoniotti, S. Paxia, M. Rejali, A. Rudra, V. Cherepinsky, N. Silver, W. Casey, C. Piazza, M. Simeoni, P. Barbano, M. Spivak, J-W. Feng, O. Gill, M. Venkatesh, F. Cheng, B. Sun, I. Ioniata, T.S. Anantharaman, E.J.A. Hubbard, A. Pnueli, D. Harel, V. Chandru, R. Hariharan, M. Wigler, F. Park, S.-C.. Lin, Y. Lazebnik, F. Winkler, C. Cantor, A. Carbone, and M. Gromov), OMICS - A Journal of Integrative Biology, (Special Issue on BioCOMP, Ed.: S. Kumar), 7(3): 253-268, 2003.
- "From Bytes to Bedside: Computational Biology for Biomedical Translational Research," (with J.P. Mathew, A. Chinnaiyan, G. Bader, S. Pyarajan, B. Taylor, M. Antoniotti, C. Sander and S.J. Burakoff), PLoS Computational Biology, 3(2): 1-12, 2007.
- "Metamorphosis: The Coming Transformation of Translational Systems Biology," (with S. Kleinberg), ACM Queue 2009.

Models of Apoptosis



- "Mathematical Modeling of the formation of Apoptosome in Intrinsic Pathway of Apoptosis," (with S. Ryu et al.), Systems and Synthetic Biology Journal, 2009.
- "The Apoptotic Machinery As A Biological Complex System: Analysis Of Its Omics And Evolution, Identification Of Candidate Genes For Fourteen Major Types Of Cancer And Experimental Validation in CML And Neuroblastoma," (with C. Di Pietro et al.), BMC Medical Genomics, 2009.

Model Checking in Biology



- "xS-systems: eXtended S-systems and Algebraic Differential Automata for Modeling Cellular Behavior," (with M. Antoniotti, A. Policriti and N. Ugel), High Performance Computing--HiPC 2002, (Eds. S. Sahni, V.K. Prasanna & U. Shukla), LNCS 2552:431-442, Springer-Verlag, December 2002.
- "Model Building and Model Checking for Biochemical Processes," (with M. Antoniotti, A. Policriti and N. Ugel), Cell Biochemistry and Biophysics (CBB), 38(3): 271-286, Humana Press, June, 2003.
- "Taming the Complexity of Biochemical Models through Bisimulation and Collapsing: Theory and Practice," (with M. Antoniotti, C.Piazza, A. Policriti and M. Simeoni), Theoretical Computer Science, 325(1): 45-67, 2004.
- "Simpathica: A Computational Systems Biology Tool within the Valis Bioinformatics Environment," (with M. Antoniotti, S. Paxia and N. Ugel), Computational Systems Biology, (Ed. E. Eiles and A. Kriete), Elsevier, 2005.
- "A Coherent Framework for Multi-resolution Analysis of Biological Networks with Memory: RAS pathway, Cell Cycle and Immune System," (with P. Barbano, M. Spivak, J. Feng, and M. Antoniotti), *Proc. National Academy of Science U S A*, 102(18):6245-6250, 2005.

Algorithmic Algebraic Model Checking



- "Algorithmic Algebraic Model Checking I: Challenges from Systems Biology," (with C. Piazza, M. Antoniotti, V. Mysore, A. Policriti, and F. Winkler), 17th International Conference on Computer Aided Verification, (The University of Edinburgh, Scotland, UK, July 6 10, 2005), CAV 2005:5-19, 2005.
- "Algorithmic Algebraic Model Checking II: Decidability of Semi-Algebraic Model Checking and its Applications to Systems Biology," (with V. Mysore and C. Piazza), Automated Technology for Verification and Analysis: (Taipei, Taiwan, October 4 - 7, 2005), ATVA 2005: 217-233, 2005.
- "Algorithmic Algebraic Model Checking III: Approximate Methods," (with V. Mysore), 7th International Workshop on Verification of Infinite-State Systems, INFINITY 05, San Francisco, California, USA, August 27, 2005. Electr. Notes Theor. Comput. Sci., 149(1):61-77, 2006.
- "Algorithmic Algebraic Model Checking IV: Characterization of Metabolic Networks," (with V. Mysore), Algebraic Biology, AB '2007, Linz, Austria, July 2007.
- "Intelligently Deciphering Unintelligible Designs: Algorithmic Algebraic Model Checking in Systems Biology," (Invited Paper), *Interface: Journal of the Royal Society*, 2009.

Optical Mapping



- "Mapping the Genome One Molecule at a Time -- Optical Mapping," (with A.H. Samad et al.), Nature, 378:516-517, 1995
- "Genomics via Optical Mapping II: Ordered Restriction Maps," (with T.S. Anantharaman and D.C. Schwartz), Journal of Computational Biology, 4(2):91-118, 1997.
- "Genomics via Optical Mapping III: Contiging Genomic DNA and Variations," (with T.S. Anantharaman and D.C. Schwartz), *Proceedings 7th Intl. Cnf. on Intelligent Systems for Molecular Biology*: ISMB '99 , 7:18-27, AAAI Press, 1999.
- "Optical Mapping and Its Potential for Large-Scale Sequencing Projects," (with C. Aston and D.C. Schwartz), Trends in Biotechnology, 17:297-302, 1999.
- "Optical Mapping," Encyclopedia of the Human Genome, 4: 448-453, Nature Publishing Group, Macmillan Publishers Limited, London, UK, June, 2003.

Copy Number Fluctuations



- "Detecting Gene Copy Number Fluctuations in Tumor Cells by Microarray Analysis of Genomic Representations," (with R. Lucito et al.), *Genome Research*, 10(11): 1726-1736, 2000.
- "Comparing Genomes," Special issue on "Biocomputation:" Computing in Science and Engineering., pp 42-49, January/February 2002.
- "A Versatile Statistical Analysis Algorithm to Detect Genome Copy Number Variation," (with R.-S. Daruwala, A. Rudra, H. Ostrer, R. Lucito, and M. Wigler), *Proc. National Academy of Science U S A*, 101(46): 16292-7, 2004.
- "Mapping Tumor Suppressor Genes using Multipoint Statistics from Copy-Number Variation Data," (with I. Ionita and R. Daruwala), American Journal of Human Genetics, 79(1):13-22, July 2006.
- "Copy Number Variant Analysis of Human Embryonic Stem Cells," (with H. Wu et al.), Stem Cells, 26(6):1484-9, June 2008.

Single Molecule/Single Cell Nanotechnology



- "Single Molecule Transcription Profiling with AFM," (with J. Reed, B. Pittenger, S. Magonov, J. Troke, M.A. Teitell, and J.K. Gimzewski), Nanotechnology, 18, 1-15, 2007.
- "Atomic Force Microscope Observation of Branching in Single Transcript Molecules Derived from Human Cardiac Muscle," (with J. Reed, C. Hsueh and J. Gimzewski), Nanotechnology, 19 384021 (8pp), 2008.
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Ontology: GOALIE



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Answer to Cancer





- "If I know the answer I'll tell you the answer, and if I don't, I'll just respond, cleverly."
 - Ex-US Secretary of Defense, Mr.
 Donald Rumsfeld.



The end